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Introduction example

Find all prime numbers from 1 to n and store them in memory.

n: data to read

Problem: choice of the data structure

If Array: not possible to define its size

If Array: not possible to precisely define its size even if n is known



Space allocation must be dynamic

Concept of Static and Dynamic Allocation

Static allocation

Space is entirely allocated at the beginning of a process

In technical terms, we describe this as the space being known at compile time

It 's therefore an array

Dynamic allocation

Space is allocated as the program executes

To perform this type of allocation, the user must have access to both space allocation and space deallocation operations.

If the programming language provides these capabilities, they can be used directly

Otherwise, simulate them, meaning managing the space manually within a large array.

Definition

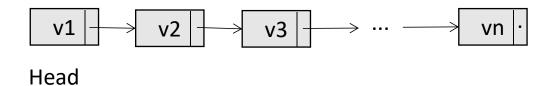
A linked list (LL) is a collection of dynamically allocated nodes (or cells) linked together

An item of an LL is always a structure with two fields:

- Value field : holding the information
- Address field : giving the address of the next cell

Each node is associated with an address

This introduces in the algorithmic language a new variable type: the POINTER type



An LL is characterized by the address of its first element.

Nil represents an address that does not point to any node

Abstract Machine (AMLL)

```
ALLOCATE _CELL( P ) :
    Create a cell and return its address in P.
FREE (P):
    Free the node of address P.
NEXT (P):
    Access to the Address field of the node referenced by P.
CELL_VALUE (P):
    Access to the Value field of the node referenced by P.
ASS_ADR ( P, Q ) :
    Assign to the Address field of the node referenced by P, the address Q.
ASS VAL(P, Val):
    Assign to the Value field of the node referenced by P, the value Val.
```

Solution to introduction problem

We use the following two facts next:

- 1. A number is prime only if it is not divisible by the prime numbers that precede it.
- 2. All prime numbers are of the form 6m+1 or 6m-1.

P Head Q Q Q 3

Solution to introduction problem

```
READ (N);
ALLOCATE_CELL(P);
ASS_VAL(P,2);
WRITE(2,3);
Head:=P;
ALLOCATE_CELL(Q);
ASS_VAL(Q,3);
WRITE(3);
ASS_ADR(Q,NULL);
ASS_ADR(P,Q);
```

Head \downarrow P \downarrow Q \downarrow 2 \rightarrow 3 \rightarrow 5

Solution to introduction problem

```
READ (N);
ALLOCATE_CELL(P);
ASS_VAL(P,2);
WRITE(2,3);
Head:=P;
ALLOCATE_CELL(Q);
ASS_VAL(Q,3);
WRITE(3);
ASS_ADR(Q,NULL);
ASS_ADR(P,Q);
```

```
M := 1; Continue := TRUE; Aig := TRUE;
WHILE Continue:
 CALL Gen_Number ( M , Aig , Number );
 Aig := NOT Aig ;
 IF Aig:
   M := M + 1
 ENDIF;
 IF Number <= N:
   IF Prime ( Head , Number ) :
     WRITE (Number); ALLOCATE CELL(Q);
     ASS_VAL(Q, Number); ASS_ADR(Q, NULL);
     ASS_ADR(P,Q);
     P := Q
   ENDIF
 ELSE
   Continue := FALSE
 ENDIF
ENDWHILE;
```

Solution to introduction problem

```
Gen_nombre( M, Aig, Number )

If Aig : Number := 6M - 1

Else Numbre := 6M + 1 Endif

Divisible (A, B)

Q := A / B {Integer division }

Divisible := Q.B = A
```

```
Prime (L, N)

P := L;

Found := FALSE;

WHILE ( P <> NULL ) AND NOT Found :

IF Divisible ( Number , CELL_VALUE ( P ) ) :

Found := TRUE

ELSE

P := NEXT ( P )

ENDIF

ENDWHILE;

Prime := NOT Found
```

Algorithms on linked lists

Just like with arrays, algorithms on LLs can be classified as follows:

- 1. Traversal: access by value, access by position
- 2. Updates: insertion, deletion
- 3. Algorithms involving multiple LLs: merging, interleaving, splitting, etc.
- 4. Sorting

Special Linked Lists

Doubly linked list (DLL)

It is an LL that can be traversed in both directions

```
AMDLL = AMLL - {ASS_ADR} + { ASS_R_ADR, ASS_L_ADR, PREVIOUS }
```

The abstract machine on LL is extended by the following operations:

```
PREVIOUS (P): Access to the 'Left address' field of the node referenced by P.

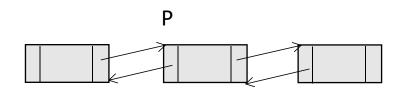
ASS_R_ADR (P, Q): Assign to the 'Right address' field of the node referenced by P, the address Q.
```

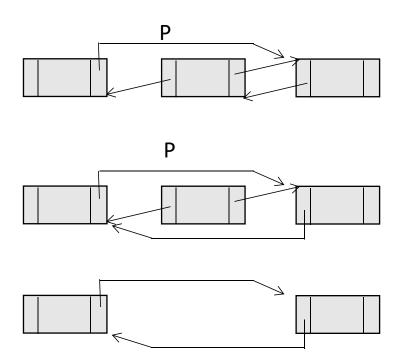
ASS_L_ADR (P, Q): Assign to the 'Left address' field of the node referenced by P, the address Q.

Special Linked Lists

Deleting the item pointed by P in a doubly linked list L

```
IF P # NULL :
    IF PREVIOUS ( P ) # NULL :
        ASS_R_ADR ( PREVIOUS ( P ) , NEXT ( P ) )
    ELSE
        L := Next (P)
    ENDIF
    IF NEXT ( P ) # NULL :
        ASS_L_ADR ( NEXT ( P ) , PREVIOUS ( P ) )
    ENDIF
    FREE ( P ) ;
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```





Special Linked Lists

Circular Linked List (CLL)

It is an LL in which the last element points to the first. It is defined by the address of any element

AMLLC = AMLL

Special Linked Lists

Circular Doubly Linked List (CDLL)

It is a two-way CLL in which the last (first) element points to the first (last)

AMCDLL = AMDLL.

Implementation: Dynamic (C)

```
#include <stdio.h>
#include <stdlib.h>
/** -Implementation- **\: LIST Of INTEGERS**/
/** Linked lists **/
typedef int Typeelem Li;
typedef struct Cell_Li * Pointer_Li ;
struct Cell Li
  Typeelem Li Val;
  Pointer_Li Next;
};
Pointer_Li Allocate_cell_Li (Pointer_Li *P)
  *P = (struct Cell_Li *) malloc( sizeof( struct Cell_Li));
  (*P)->Next = NULL;
void Ass val Li(Pointer Li P, Typeelem Li Val)
  P->Val = Val;
```

```
void Ass adr Li(Pointer Li P, Pointer Li Q)
  P->Next = Q;
Pointer Li Next Li( Pointer Li P)
 { return( P->Next ); }
Typeelem Li Cell value Li(Pointer Li P)
 { return( P->Val) ; }
void Free Li (Pointer Li P)
 { free (P);}
/** Variables of main program **/
Pointer Li L=NULL;
int main(int argc, char *argv[])
  system("PAUSE");
  return 0;
```

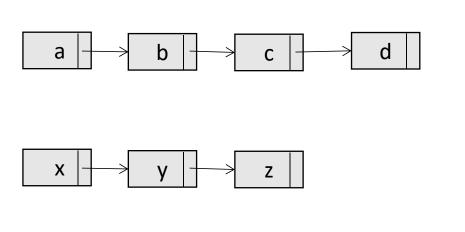
Implementation: Static (C)

The array is a set of triples (Element, Next, Occupied)

The 'Element' field holds the stored value.

The 'Next' field contains the address of the next cell.

The 'Occupied' field indicates the availability of the cell. It is necessary for 'Allocate' and 'Free' operations.



Static (or global) Array

У	6	V
d	-1	V
b	5	V
а	2	V
X	0	V
С	1	V
Z	-1	V
		F
		F

0

Max -1

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Implementation: Static (C)

Linked lists can be represented in a single array

An initialization phase is mandatory before using this array. It consists of initializing the 'Occupied' field to false.

A linked list is defined by the index of its first element.

```
#define Max 100
#define True 1
#define False 0
#define Nil -1

typedef int Bool;
typedef int Anytype;
struct Typelist
{
    Anytype Element;
    int Next;
    Bool Occupied;
};
struct Typelist List[ Max ];
```

Implementation: Static (C)

```
void Allocate ( int *I )
  Bool Found;
  *I = 0;
  Found = False;
  while (*I < Max && !Found)
   if ( List[*I].Occupied )
    *|++;
   else
    Found= True;
   if (!Found) *I = -1;
void Free ( int I )
  List[I].Occupied = False ;
Anytype Value (int I)
  return( List[I].Element );
```

```
int Next (int I)
  return ( List[I].Next );
void Ass_val ( int I, Anytype Val)
  List[I].Element = Val;
void Ass_adr ( int I, int J)
  List[I].Next = J;
int main(int argc, char *argv[])
  system("PAUSE");
  return 0;
```

Implementation: Dynamic (Pascal)

```
PROGRAM My program;
{ -Implementation- : LIST Of INTEGERS}
{ Linked lists }
TYPE
 Typeelem LI = INTEGER;
 Pointer_LI = ^Cell_LI; { type of field 'Address' }
 Cell LI = RECORD
   Val: Typeelem LI;
   Next: Pointer LI
 END;
PROCEDURE Allocate cell LI (VAR P: Pointer LI);
 BEGIN NEW(P) END;
PROCEDURE Free LI (P: Pointer LI);
 BEGIN DISPOSE(P) END;
PROCEDURE Ass val LI(P: Pointer LI; Val: Typeelem LI);
 BEGIN
  P^.Val := Val
 END;
```

```
FUNCTION Cell_value_LI (P : Pointer_LI) : Typeelem_LI;
 BEGIN Cell value LI := P^.Val END;
FUNCTION Next LI(P: Pointer LI): Pointer LI;
 BEGIN Next LI := P^.Next END;
PROCEDURE Ass adr LI(P, Q: Pointer LI);
 BEGIN P^.Next:= Q END;
{ Declaration part of variables }
VAR
 L : Pointer LI;
{ Body of main program }
BEGIN
 READLN;
END.
```